

Progression of Skills

Representations

Add 1s, 10s and 100s to a 4-digit number

Emphasis on mental strategies including number bonds and related facts. Prompt children to notice which digit changes.

The ones/tens/hundreds/thousands column will increase by ...



$$3,425 + 3 = \quad 3,425 + 300 =$$

$$3,425 + 30 = \quad 3,425 + 3,000 =$$

What patterns do you notice?

$$2,350 + 3 =$$

$$2,350 + 30 =$$

$$2,350 + 300 =$$

$$2,350 + 3,000 =$$

$$6,040 + 200 = \quad 2,211 + \boxed{} = 2,251$$

$$6,040 + 500 = \quad 2,211 + \boxed{} = 2,215$$

$$6,040 + 900 = \quad 2,211 + \boxed{} = 2,511$$

Add up to two 4-digit numbers

Formal written method with up to 3 exchanges. Encourage children to estimate and use inverse operations to check answers to calculations.

There are ... ones/tens/hundreds so I do/do not need to make an exchange.

I can exchange 10 ... for 1 ...



	4	6	7	3	
+	1	5	1	8	
	1		1		
	6	1	9	1	

Add decimal numbers in the context of money

Emphasis on partitioning and use of number lines rather than formal written calculations.

... pence + ... pence = ... pence
... pounds + ... pounds = ... pounds



$$45\text{p} + 25\text{p} = 70\text{p}$$

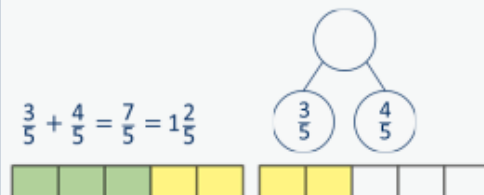
$$£2 + £3 = £5$$

$$£5 + 70\text{p} = £5.70$$

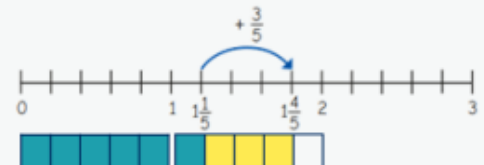
£3.25 can be partitioned into £3 + 20p + 5p

**Add fractions and mixed numbers with the same denominator beyond 1 whole**

When adding fractions with the same denominator, I only add the numerator.
... fifths + ... fifths = ... fifths



$$\frac{3}{5} + \frac{4}{5} = \frac{7}{5} = 1\frac{2}{5}$$



Subtract numbers with up to 4 digits using a formal written method.

Solve simple measure and money problems involving fractions and decimals to 2 decimal places.

Subtract fractions with the same denominator.

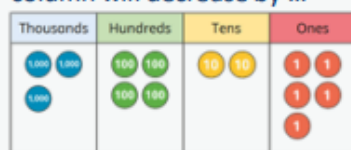
Representations

Progression of Skills

Subtract 1s, 10s, 100s and 1,000s from a 4-digit number

Emphasis on mental strategies including number bonds and related facts. Prompt children to notice which digit changes.

The ones/tens/hundreds/thousands column will decrease by ...



$$3,425 - 2 = \quad 3,425 - 200 = \quad$$

$$3,425 - 20 = \quad 3,425 - 2,000 = \quad$$

What patterns do you notice?

$$4,356 - 3 =$$

$$4,356 - 30 =$$

$$4,356 - 300 =$$

$$4,356 - 3,000 =$$

$$6,940 - 200 =$$

$$6,940 - 300 =$$

$$6,940 - 400 =$$

$$4,433 - \square = 4,430$$

$$4,433 - \square = 4,033$$

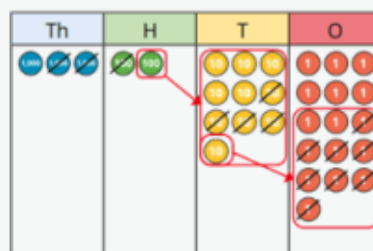
$$4,433 - \square = 4,403$$

Subtract up to two 4-digit numbers

Formal written method with up to 3 exchanges. Encourage children to estimate and use inverse operations to check answers to calculations.

I need to subtract... ones/tens/hundreds. I do/do not need to make an exchange.

I can exchange 1... for 10...



	Th	H	T	O
	3	2	5	6
-	2	1	4	8
	1	0	5	8

Subtract decimal numbers in the context of money

Emphasis here is on partitioning and use of number lines rather than formal written calculations.

I can partition £... into £... and 100p
 $\pounds \dots - \pounds \dots = \pounds \dots$
 $100\text{p} - \dots\text{p} = \dots\text{p}$

$$\pounds 5 - \pounds 3.26$$

$$\pounds 4 - \pounds 3 = \pounds 1$$

$$100\text{p} - 26\text{p} = 74\text{p}$$

$$\pounds 5 - \pounds 3.26 = \pounds 1.74$$

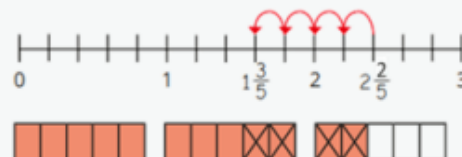
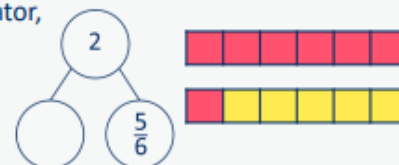
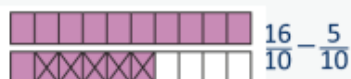


£3.26 can be partitioned into £3 + 20p + 6p

**Subtract fractions and mixed numbers with the same denominator**

Include subtracting fractions from wholes.

When subtracting fractions with the same denominator,
 I only subtract the numerator.
 ... tenths - ... tenths = ... tenths



Recall multiplication facts for multiplication tables up to 12×12

Use place value, known and derived facts to multiply mentally, including: multiplying by 0 and 1; multiplying together three numbers.

Recognise and use factor pairs and commutativity in mental calculations.

Multiply two-digit and three-digit numbers by a one-digit number using formal written layout.

Solve problems involving multiplying and adding, including using the distributive law to multiply two-digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects.

Progression of Skills

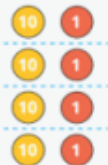
Times-table facts to 12×12

Encourage daily counting in multiples both forwards and back. Encourage children to notice links between related times-tables.

Representations

... groups of ... =
... times ... is equal to ...

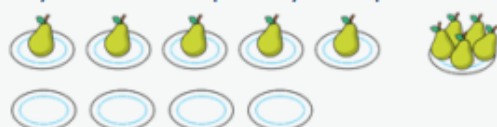
... \times ... =



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Multiply by 1 and 0

Any number multiplied by 1 is equal to ...
Any number multiplied by 0 is equal to ...



... \times ... = ...

$$\begin{array}{ll} 1 \times 1 = 1 & 1 \times 0 = 0 \\ 2 \times 1 = 2 & 2 \times 0 = 0 \\ 3 \times 1 = 3 & 3 \times 0 = 0 \\ 4 \times 1 = 4 & 4 \times 0 = 0 \end{array}$$

Multiply 3 numbers

Children use their understanding of commutativity to multiply more efficiently.

To work out ... \times ... \times ..., I can first calculate ... \times ... and then multiply the answer by ...

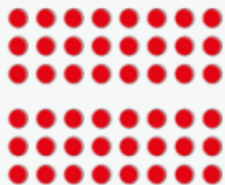


$$\begin{array}{l} 4 \times 2 \times 3 = 8 \times 3 = 24 \\ 2 \times 3 \times 4 = 6 \times 4 = 24 \\ 3 \times 4 \times 2 = 12 \times 2 = 24 \end{array}$$

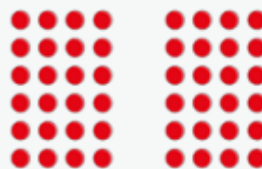
Factor pairs

Children explore equivalent calculations using different factors pairs.

$12 = \dots \times \dots$, so ... $\times 12 = \dots \times \dots \times \dots$



$$\begin{array}{l} 8 \times 6 = 8 \times 3 \times 2 \\ 8 \times 6 = 24 \times 2 \end{array}$$

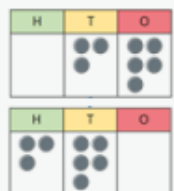


$$\begin{array}{l} 6 \times 8 = 6 \times 4 \times 2 \\ 6 \times 8 = 24 \times 2 \end{array}$$

Multiply by 10 and 100

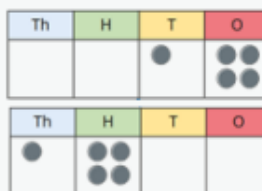
Some children may over-generalise that multiplying by 10 or 100 always results in adding zeros. This will cause issues later when multiplying decimals.

When I multiply by 10, the digits move ... place value column to the left.
... is 10 times the size of ...



$$35 \times 10 = 350$$

When I multiply by 100, the digits move ... place value columns to the left.
... is 100 times the size of ...



$$14 \times 100 = 1,400$$

Related facts

Use knowledge of multiplying by 10 and 100 to scale times-table facts.

... \times ... ones is equal to ... ones
so ... \times ... tens is equal to ... tens
and ... \times ... hundreds is equal to ... hundreds.



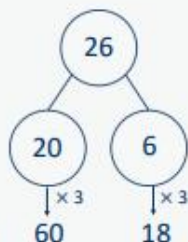
$$\begin{aligned} 3 \times 7 &= 21 \\ 3 \times 70 &= 210 \\ 3 \times 700 &= 2,100 \end{aligned}$$

$$\begin{aligned} 7 \times 3 &= 21 \\ 7 \times 30 &= 210 \\ 7 \times 300 &= 2,100 \end{aligned}$$

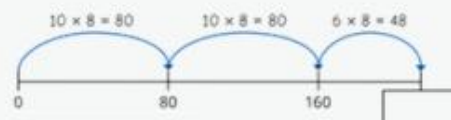
Mental strategies

Partition 2 or 3-digit numbers to multiply using informal methods.

... tens multiplied by ... is equal to ... tens.
...ones multiplied by ... is equal to ... ones.



$$3 \times 26 = 60 + 18 = 78$$

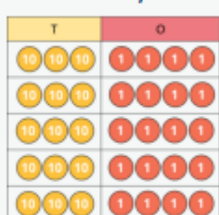


$$26 \times 8 = 80 + 80 + 48 = 208$$

Multiply a 2 or 3-digit number by a 1-digit number

The short multiplication method is introduced for the first time, initially in an expanded form.

To multiply a 2-digit number by ... , I multiply the ones by ... and the tens by ...
To multiply a 3-digit number by ... , I multiply the ones by ... , the tens by ... and the hundreds by ...



	H	T	O	
		3	4	
x			5	
		2	0	5 x 4
	1	5	0	5 x 30
	1	7	0	

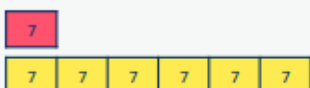
	H	T	O	
		3	4	
x			5	
	1	2		
	1	7	0	



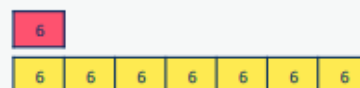
Scaling

Children focus on multiplication as scaling (... times the size).

... is ... times the size of ...



A computer mouse costs £7
A keyboard costs 6 times as much.



A red ribbon is 6 cm.
A yellow ribbon is 7 times as long.

Correspondence problems

Encourage children to use tables to show all the different possible combinations.

For every ... , there are ... possibilities.
There are ... \times ... possibilities altogether.

A pizza company offers a choice of 5 toppings and 3 bases.

$$5 \times 3 = 15$$

	Deep pan	Italian	Thin
Cheese	C DP	C I	C Th
Mushroom	M DP	M I	M Th
Vegetable	V DP	V I	V Th
Chicken	C DP	C I	C Th
Tuna	T DP	T I	T Th

Recall division facts for multiplication tables up to 12×12

Use place value, known and derived facts to divide mentally, including: dividing by 1

Find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths.

Division facts to 12×12

Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.

There are ... groups of ... in ...

$$\dots \div \dots =$$



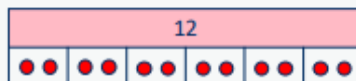
$$2 \times 6 = 12$$

$$12 \div 6 = 2$$



... has been shared equally into ... equal groups.

$$\dots \div \dots =$$



$$2 \times 6 = 12$$

$$12 \div 6 = 2$$

Divide a number by 1 and itself

Children may try to divide a number by zero and it should be highlighted that this is not possible.

Related facts

Link to known times-table facts.

When I divide a number by 1, the number remains the same.

5 shared between 1 is 5



There are 5 groups of 1 in 5

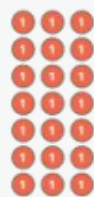


When I divide a number by itself, the answer is 1

5 shared between 5 is 1



There is 1 group of 5 in 5

... \div ... is equal to ...so ... tens \div ... is equal to ... tensand ... hundreds \div ... is equal to ... hundreds.

$$21 \div 7 = 3$$

$$210 \div 7 = 30$$

$$2,100 \div 7 = 300$$

$$21 \div 3 = 7$$

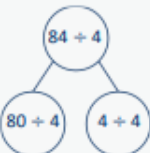
$$210 \div 3 = 70$$

$$2,100 \div 3 = 700$$

Divide a 2 or 3-digit number by a 1-digit number

Progress from divisions with no exchange, to divisions with exchange and then divisions with remainders.

I can partition ... into ... tens and ... ones.



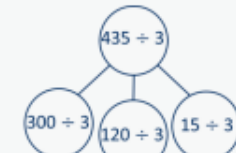
$$80 \div 4 = 20$$

$$4 \div 4 = 1$$

$$84 \div 4 = 21$$

Tens	Ones
20	1
20	1
20	1
20	1

I cannot share the hundreds/tens equally, so I need to exchange 1 ... for 10 ...



$$300 \div 3 = 100$$

$$120 \div 3 = 40$$

$$15 \div 3 = 5$$

$$435 \div 3 = 145$$

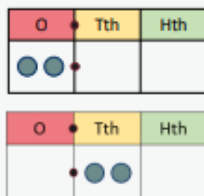
Hundreds	Tens	Ones
100	40	5
100	40	5
100	40	5
100	40	5

Divide by 10 and 100

Encourage children to notice that dividing by 100 is the same as dividing by 10 twice.

When I divide by 10, the digits move 1 place value column to the right.

... is one-tenth the size of ...



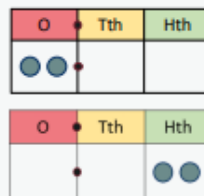
$$2 \div 10 = 0.2$$



$$12 \div 10 = 1.2$$

When I divide by 100, the digits move 2 place value columns to the right.

... is one-hundredth the size of ...



$$2 \div 100 = 0.02$$



$$12 \div 100 = 0.12$$