

Recall and use addition facts to 20 fluently, and derive and use related facts up to 100

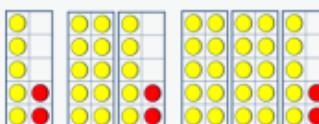
- Add numbers using concrete objects, pictorial representations, and mentally, including:
  - a two-digit number and 1s
  - a two-digit number and 10s
  - 2 two-digit numbers
  - adding 3 one-digit numbers
- Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.

### Progression of skills

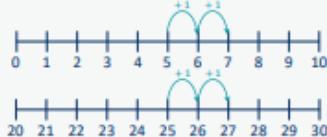
#### Add ones to any number (related facts)

Make links to known facts.

I know that ... and ... = ...  
so ... and ... = ...



... more than ... is ...  
so ... more than ... is ...



What do you notice?  
Can you continue the pattern?

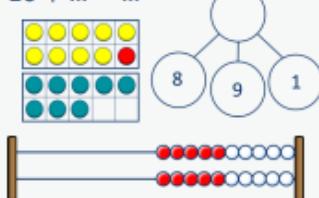
$$\begin{aligned} 5 + 2 &= 7 \\ 15 + 2 &= 17 \\ 25 + 2 &= 27 \dots \end{aligned}$$

#### Add three 1-digit numbers

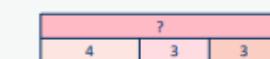
Prompt children to understand that addition can be done in any order and to make links to known facts.

... and ... are a bond to 10

$$10 + \dots = \dots$$



Double ... + ... = ...



What do you notice?  
Which addition is the easiest to calculate?

$$\begin{aligned} 8 + 9 + 1 &= \\ 8 + 1 + 9 &= \\ 9 + 1 + 8 &= \end{aligned}$$

#### Add across a 10

Partition the number being added to make a full ten.

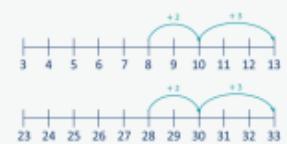
... can be partitioned into ... and ...



I add ... to get to ... then I add ...



$$\begin{aligned} 8 + 5 &= 13 \\ 28 + 5 &= 33 \end{aligned}$$



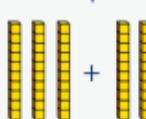
$$\begin{aligned} 8 + 5 &= 13 \\ 28 + 5 &= 33 \end{aligned}$$

#### Add multiples of 10

Make links to known facts within ten.

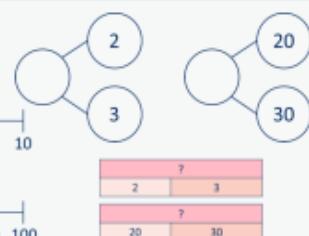
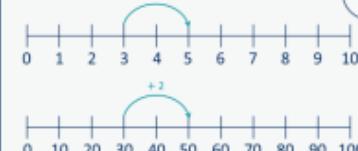
... ones + ... ones = ... ones  
so ... tens + ... tens = ... tens

$$\blacksquare \blacksquare + \blacksquare \blacksquare$$



$$\begin{aligned} 3 + 2 &= 5 \\ 30 + 20 &= 50 \end{aligned}$$

What is the same?  
What is different?



$$\begin{aligned} 2 + 3 &= 5 \\ 20 + 30 &= 50 \end{aligned}$$

#### Add 10s to any number

Make links to known facts.

... tens + ... tens = ... tens

... tens and ... ones = ...



To add ... I need to add 10 ... times.

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60

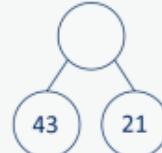
I know that ... and ... = ...  
so ... and ... = ...

$$\begin{aligned} 30 + 20 &= 50 \\ 34 + 20 &= 54 \end{aligned}$$

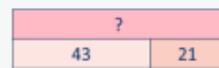
#### Add 2-digit numbers (not across a ten)

Lining up ones and tens in columns will support with later written methods.

... ones + ... ones = ... ones  
... tens + ... tens = ... tens



$$\begin{aligned} 3 \text{ ones} + 1 \text{ one} &= 4 \text{ ones} \\ 4 \text{ tens} + 2 \text{ tens} &= 6 \text{ tens} \\ 6 \text{ tens} + 4 \text{ ones} &= 64 \end{aligned}$$

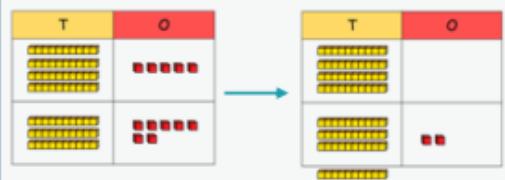


### Add 2-digit numbers (across a ten)

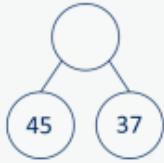
Begin to exchange 10 ones  
for 1 ten.

There are .... ones, so I do/do not need to make an exchange.

... ones = ... ten and ... ones



?	
45	37



$$\begin{aligned}5 \text{ ones} + 7 \text{ ones} &= 12 \text{ ones} \\12 \text{ ones} &= 1 \text{ ten and } 2 \text{ ones} \\4 \text{ tens} + 3 \text{ tens} + 1 \text{ ten} &= 8 \text{ tens} \\8 \text{ tens and } 2 \text{ ones} &= 82\end{aligned}$$

### Missing numbers

Solve missing number problems and use the inverse to check.

How many more do you  
need to make ...?

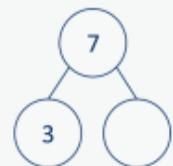
$$\begin{array}{|c|c|c|} \hline \text{Red dots} & \text{Empty boxes} & \text{Total} \\ \hline 6 & 4 & 10 \\ \hline \end{array} \quad 6 + \square = 10$$

$$10 - \square = 6$$

If ... is a whole and ... is a  
part, then ... is the other  
part.

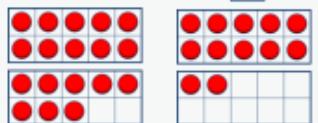
$$\begin{array}{|c|c|c|} \hline \text{Empty boxes} & \text{Whole} & \text{Part} \\ \hline 4 & 7 & 3 \\ \hline \end{array} \quad \square + 3 = 7$$

$$7 - 3 = \square$$



... can be partitioned into ...  
and ...

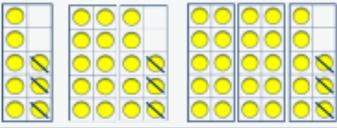
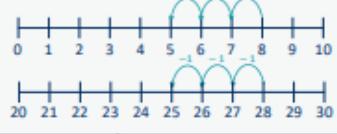
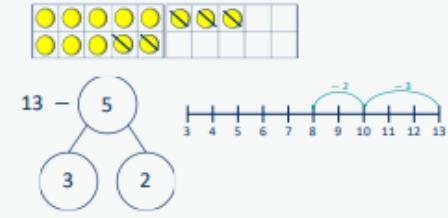
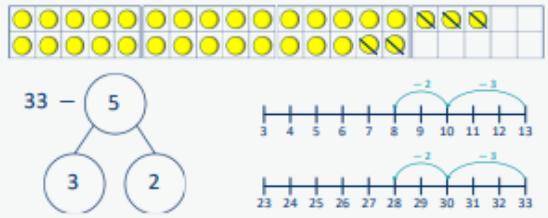
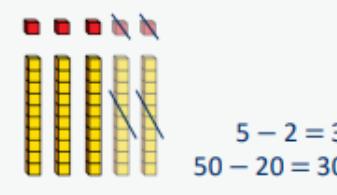
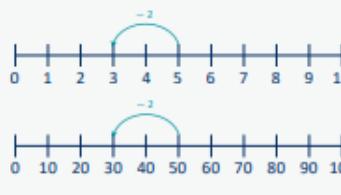
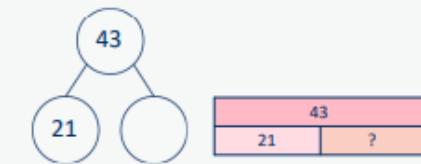
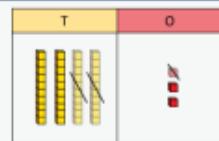
$$10 + 8 = 12 + \square$$



Recall and use subtraction facts to 20 fluently, and derive and use related facts up to 100  
 Subtract numbers using concrete objects, pictorial representations, and mentally, including:  
 • a two-digit number and 1s  
 • a two-digit number and 10s  
 • 2 two-digit numbers Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.

## Progression of Skills

## Representations

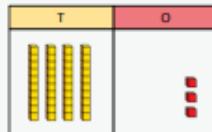
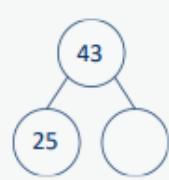
<b>Subtract ones from any number (related facts)</b>  Make links to known facts.	I know that ... minus ... = ... so ... minus ... = ...  	... less than ... is ... so ... less than ... is ...  	What do you notice? Can you continue the pattern?  $8 - 3 = 5$ $18 - 3 = 15$ $28 - 3 = 25\ldots$
<b>Subtract across a 10</b>  Partition the number being subtracted to bridge through a ten.	... can be partitioned into ... and ...  	Make links with related facts.	
<b>Subtract multiples of 10</b>  Make links to known facts within ten.	... ones - ... ones = ... ones so ... tens - ... tens = ... tens  	What is the same? What is different?	
<b>Subtract 10s from any number</b>  Make links to known facts.	... tens - ... tens = ... tens ... tens and ... ones = ...	To subtract ... I need to subtract 10 ... times.	I know that ... minus ... = ... so ... minus ... = ...  $50 - 20 = 30$ $54 - 20 = 34$
<b>Subtract two 2-digit numbers (not across a ten)</b>	... ones - ... ones = ... ones ... tens - ... tens = ... tens  		$3 \text{ ones} - 1 \text{ one} = 2 \text{ ones}$ $4 \text{ tens} - 2 \text{ tens} = 2 \text{ tens}$ $2 \text{ tens and 2 ones} = 22$

**Subtract two 2-digit numbers (across a ten)**

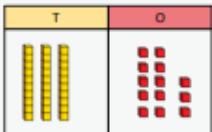
Begin to exchange 1 ten for 10 ones.

I need to make an exchange because I do not have enough ones to subtract ... ones.

43	
25	?



3 ones – 5 ones  
(I need to exchange 1 ten for 10 ones)



$$13 \text{ ones} - 5 \text{ ones} = 8 \text{ ones}$$

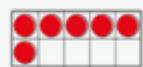
$$3 \text{ tens} - 2 \text{ tens} = 1 \text{ ten}$$

$$1 \text{ ten and } 8 \text{ ones} = 18$$

**Missing numbers**

Solve missing number problems and use the inverse to check.

How many do you need to subtract to make ...?



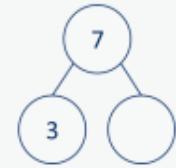
$$10 - \square = 6$$

$$6 + \square = 10$$

If ... is a whole and ... is a part, then ... is the other part.

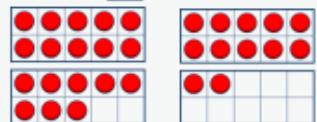
$$7 - 3 = \square$$

$$\square + 3 = 7$$



... can be partitioned into ... and ...

$$18 - \square = 12 + 2$$





### The 5 times-table

Encourage daily counting in multiples both forwards and back. Notice the pattern in the numbers.

... lots of 5 =

$\dots \times 5 =$



5	5	5	5	5
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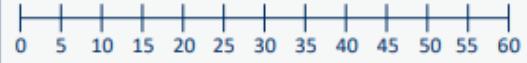
... times 5 is equal to ...

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40

$$1 \times 5 = 5 \quad 5 = 1 \times 5$$

$$2 \times 5 = 10 \quad 10 = 2 \times 5$$

$$3 \times 5 = 15 \quad 15 = 3 \times 5$$

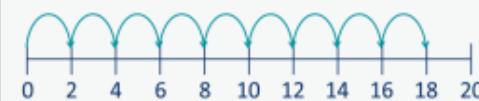


### Missing numbers

Make links to known facts.

... is equal to ... groups of ...

18 socks, how many pairs?



... times ... is equal to ...

$$\square \times 2 = 18$$

$$18 = 2 \times \square$$

Recall and use division facts for the 2, 5 and 10 multiplication tables. Calculate mathematical statements for division within the multiplication tables and write them using the division ( $\div$ ) and equals ( $=$ ) signs.

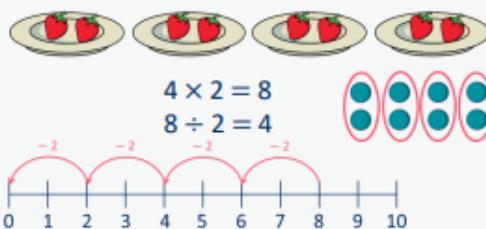
Recognise, find, name and write fractions  $\frac{1}{3}$ ,  $\frac{1}{4}$ ,  $\frac{2}{4}$  and  $\frac{3}{4}$  of a quantity.

### Divide by 2

Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts and halving.

There are ... equal groups of 2

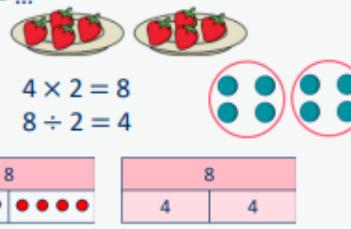
$$\dots \div 2 = \dots$$



... shared equally between 2 is ...

Half of ... is ...

$$\dots \div 2 = \dots$$



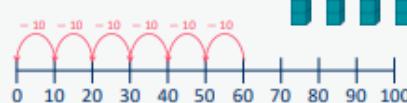
### Divide by 10

Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.

There are ... equal groups of 10

$$\dots \div 10 = \dots$$

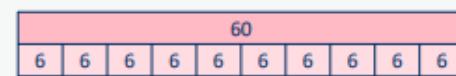
$$6 \times 10 = 60  
60 \div 10 = 6$$



... shared equally between 10 is ...

$$\dots \div 10 = \dots$$

$$6 \times 10 = 60  
60 \div 10 = 6$$

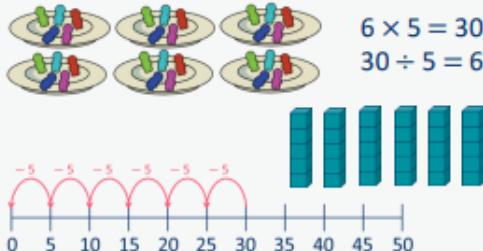


### Divide by 5

Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.

There are ... equal groups of 5

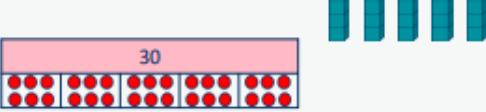
$$\dots \div 5 = \dots$$



... shared equally between 5 is ...

$$\dots \div 5 = \dots$$

$$6 \times 5 = 30  
30 \div 5 = 6$$



### Missing numbers

Bar models are useful to show the link between multiplication and division.

... divided by 2/5/10 is equal to ...

$$\begin{array}{c} ? \\ \hline 10 & 10 \end{array} \quad \square \div 2 = 10$$

$$\begin{array}{c} ? \\ \hline 10 & 10 & 10 & 10 & 10 \end{array} \quad \square \div 5 = 10$$

$$\begin{array}{c} ? \\ \hline 10 & 10 & 10 & 10 & 10 & 10 & 10 & 10 & 10 \end{array} \quad \square \div 10 = 10$$

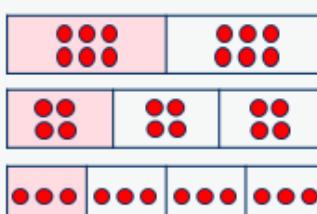
### Unit fractions

In Y2 the focus is on finding  $\frac{1}{2}$ ,  $\frac{1}{4}$  and  $\frac{1}{3}$

Bar models are useful to show the link between division and finding a fraction.

The objects have been shared fairly into ... groups.

$$\frac{1}{\square} \text{ of ... is ...}$$



There are ... equal parts.  
There is ... part circled.

$$\frac{1}{\square} \text{ is circled.}$$



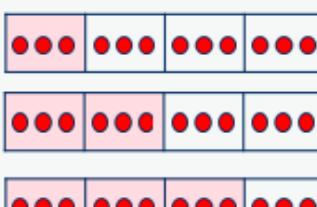
### Non-unit fractions

In Y2 the focus is on finding  $\frac{2}{4}$  and  $\frac{3}{4}$

Prompt children to notice that  $\frac{2}{4}$  is equivalent to  $\frac{1}{2}$

The objects have been shared fairly into ... groups.

$$\frac{\square}{\square} \text{ of ... is ...}$$



There are ... equal parts.  
There are ... parts circled.

$$\frac{\square}{\square} \text{ is circled.}$$

